

# **Numerical investigation on multiclass probabilistic classification of damage location in a plate structure**

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# Problem statement

International Conference on Structural  
Engineering Dynamics ICEDyn 2017  
Ericeira, Portugal, 3-5 July 2017



taken from [www.ptclwg.com](http://www.ptclwg.com)



taken from [www.rbengineering.com](http://www.rbengineering.com)

## Solution

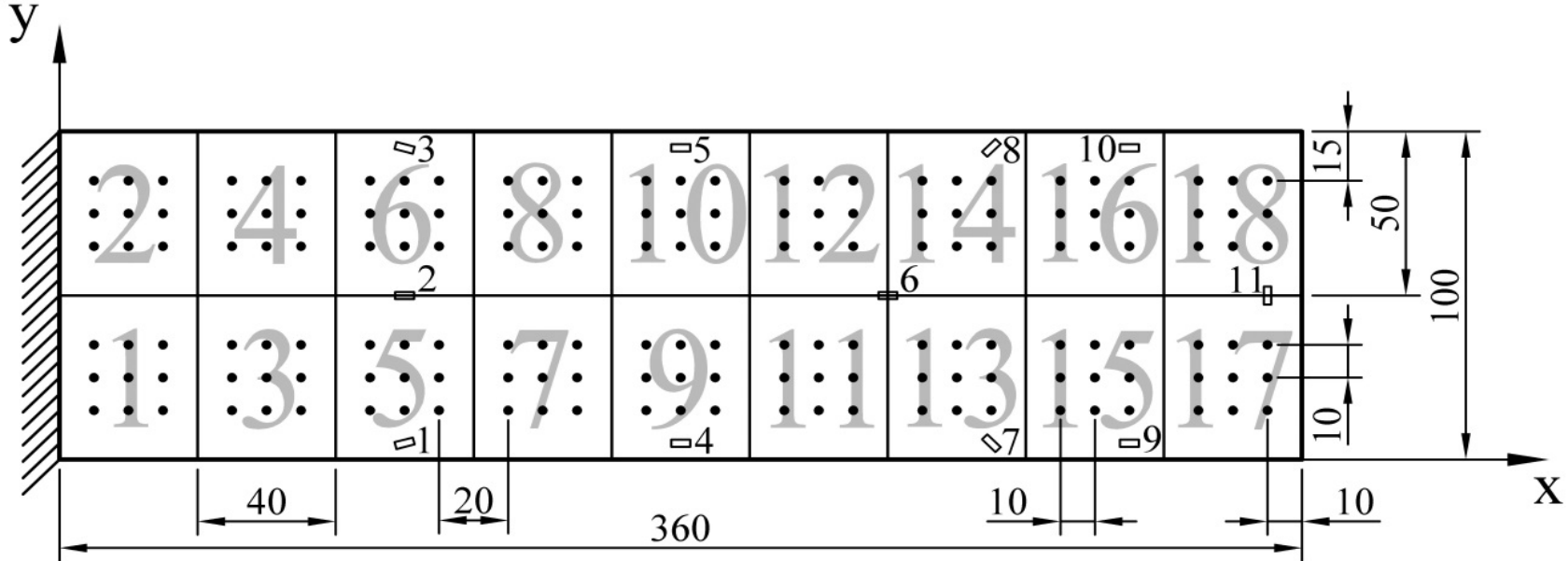
*nondestructive structural health monitoring methods*

## Damage localisation in thin composite structures based on machine learning algorithms



***k*- nearest neighbours**

**Decision trees**



- **cantilevered CFRP plate** (360 x 10 x 2.4 mm)
- **Laminate lay-up**  $[90/90/0/0/45/45/-45/-45/-45/45/0/90]_s$
- $E_x = 110 \text{ GPa}$ ,  $E_y = 7 \text{ GPa}$ ,  $G_{xy} = G_{yz} = 4.5 \text{ GPa}$ ,  $\nu_{xy} = 0.33$ ,  $\rho = 1560 \text{ kg/m}^3$ .
- **11 strain sensors**

**ANSYS model** – 8-node shear deformable shell elements  
(72 x 20 elements)

**Damage** – an artificial mass with 5 % and 10 % fractions of plate's mass is placed at selected nodes of the plate. Additional mass is applied by using **MASS21 finite element**.

Modal analysis (block Lanczos method) to extract **4** eigenfrequencies and eigenmodes.

Class labels

Plate is partitioned into 18 zones

Training

Damage is applied to 9 points in each zone

Data set

*Predictors*

18 x 9 = 162 data sets with 11 strain values



# Damage localization

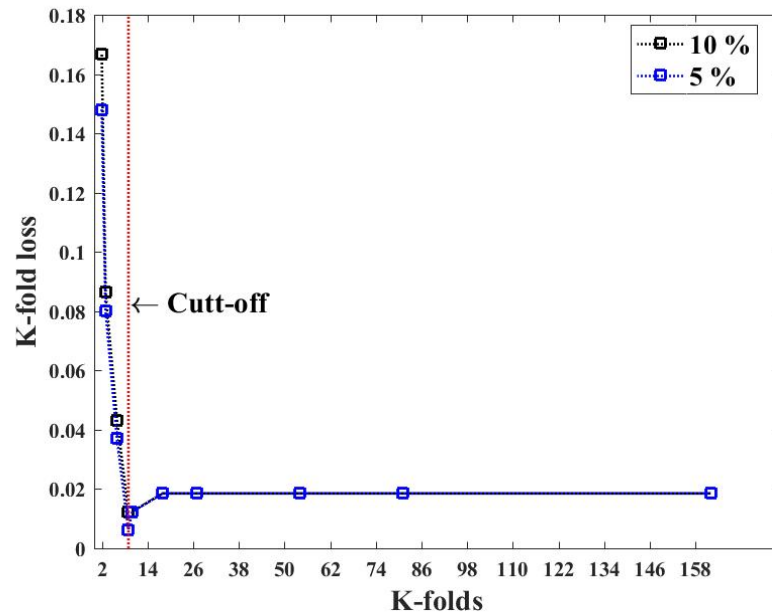
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Input strain values for each subzone	→	162 subzones × 11 strain sensors
Build a classification model	→ →	$k$ -NN (define $k$ and distance) decision trees (define max number of splits)
Calculate resubstitution loss	→ →	$k$ -NN (update $k$ and distance to yield minimum) decision trees (update max number of splits to yield minimum)
Cross-validate the model	→	$k$ -NN and decision trees (update $K$ to yield min cross-validation error)
Make prediction for future data	→ →	Compute <b>confusion matrix</b> and <b>ROC curve</b> Estimate posterior probabilities
Classify new unknown data in terms of affiliation to any of 18 zones	→ →	Perform $k$ -NN search Build a decision tree
Make a decision regarding location of damage based on majority voting for 5 % and 10 % damage severities		

# RESULTS

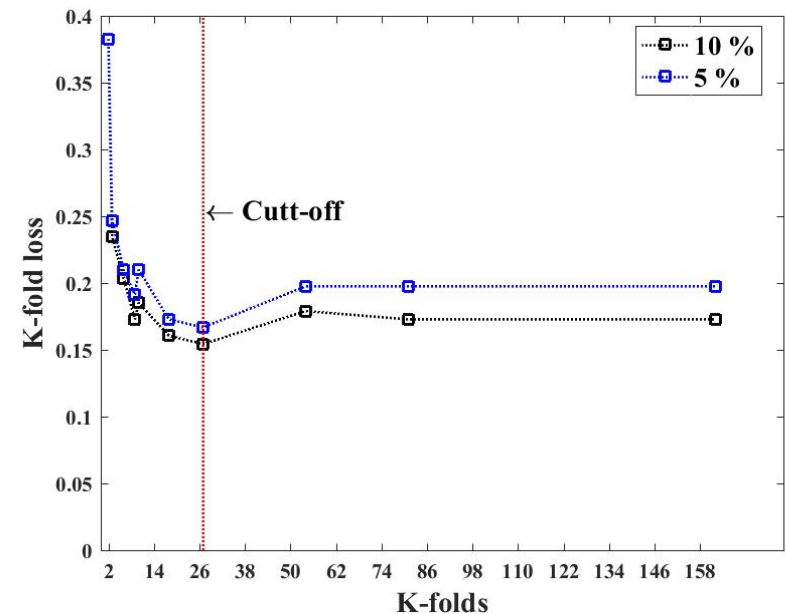


## $k$ -NN

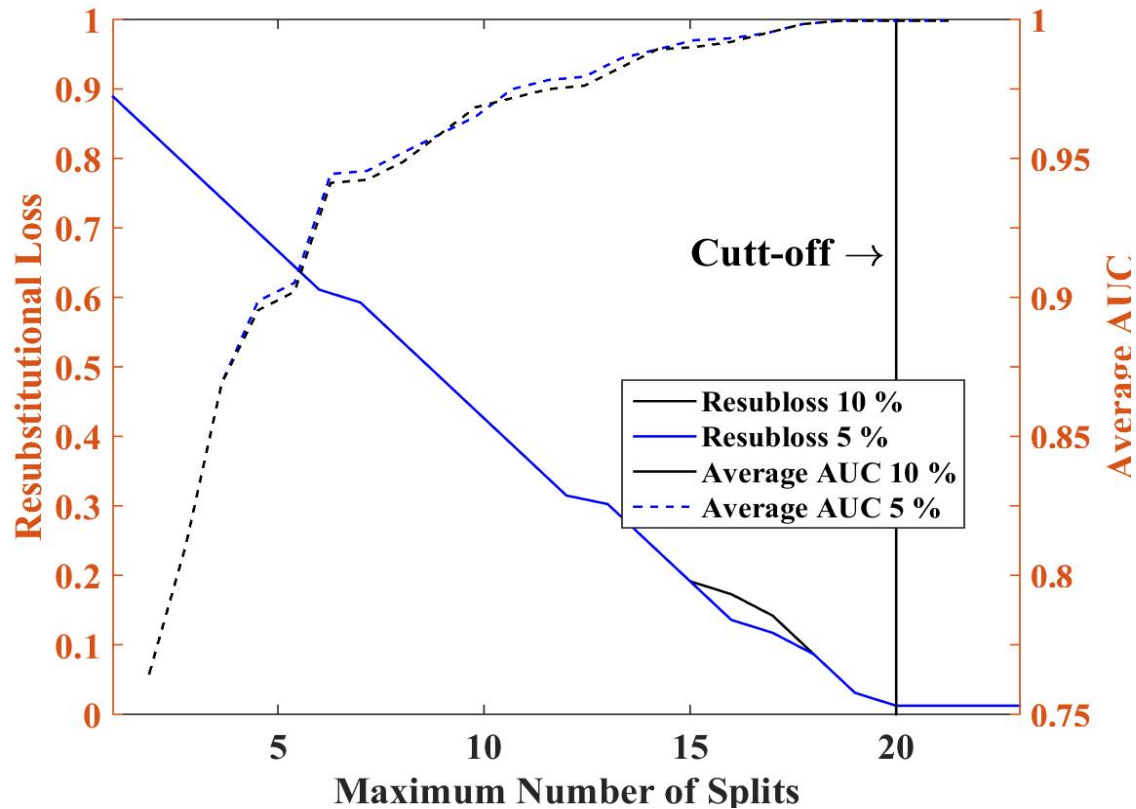


Damage severity	10 %	5 %
Number of K-folds	9	9
K-fold loss (%)	0.62	0.62

## Decision trees



Damage severity	10 %	5 %
Number of K-folds	27	27
K-fold loss (%)	15.43	16.67



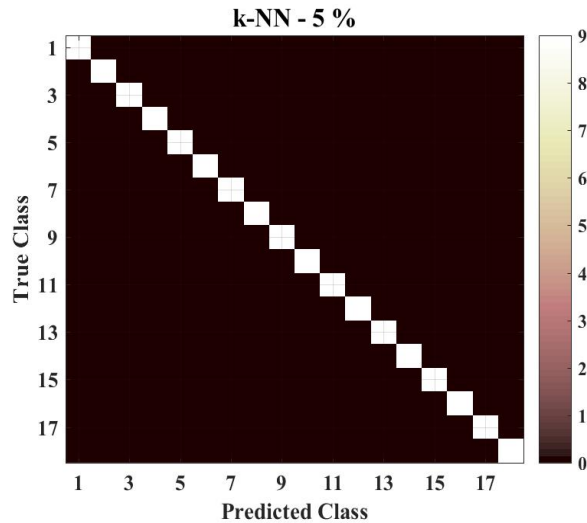
***k*-NN**

Damage severity	10 %	5 %
<i>k</i>	3	3
Resubstitution loss (%)	0	0

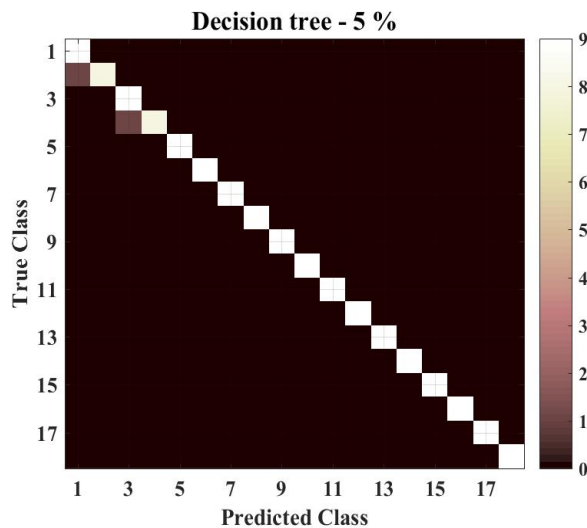
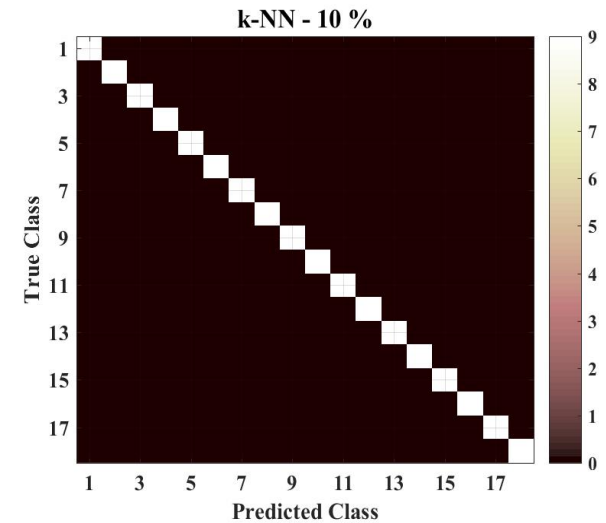
**Decision trees**

Damage severity	10 %	5 %
Maximum number of splits	3	3
Resubstitution loss (%)	1.23	1.23

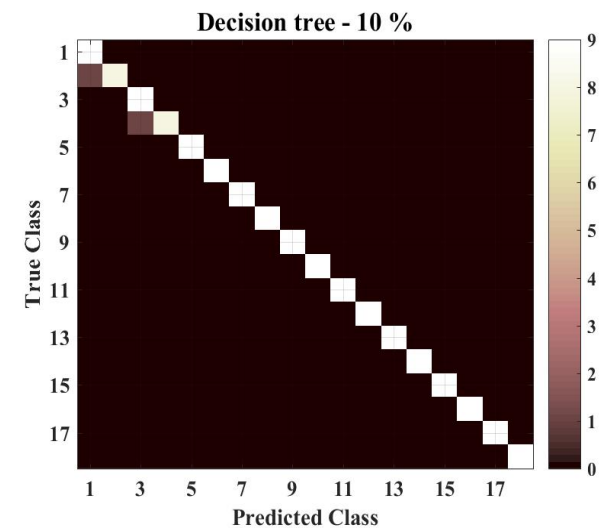
# Confusion matrix



A perfect classification for  
both damage severities



A slight misclassification in  
classes no. 2 and 4

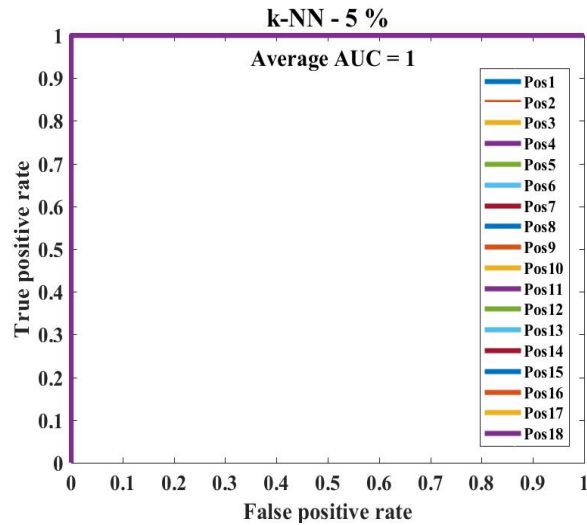




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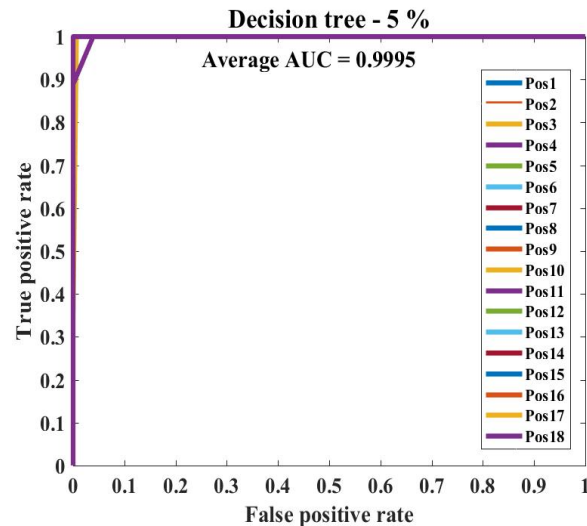
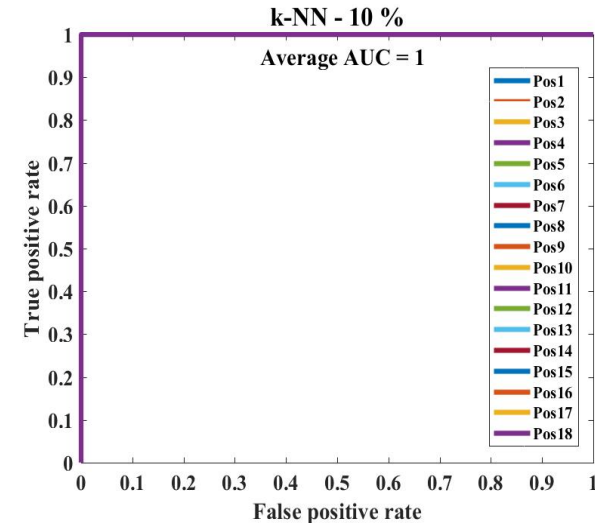
# ROC curves

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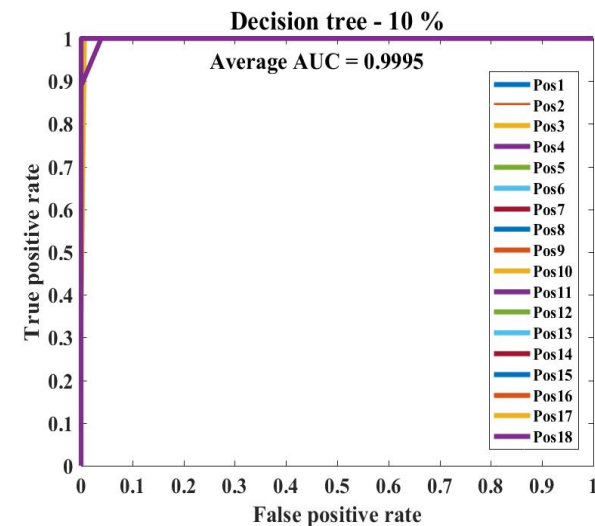


ROC curves are computed  
for each of 18 classes

AUC is equal to 1



AUC values for all classes  
are 1, except for classes no.  
1, 2, 3 and 4.



2 new points subjected to classification with k-NN and decision trees

Damage severity 10 %				Damage severity 5 %			
$X_1$	0.34	$Y_1$	0.005	$X_1$	0.13	$Y_1$	0.035
$X_2$	0.2	$Y_2$	0.05	$X_2$	0.32	$Y_2$	0.07

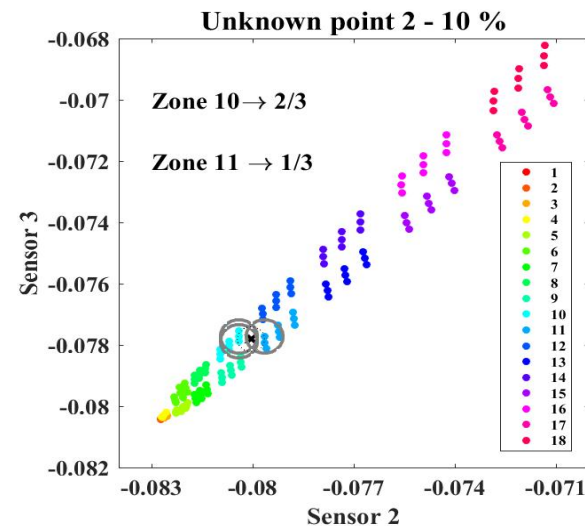
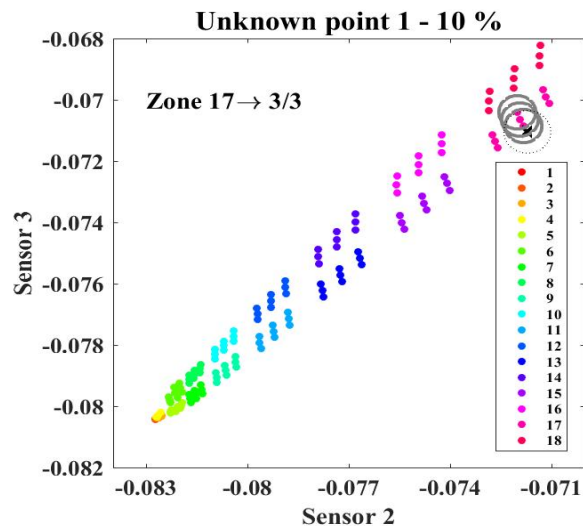
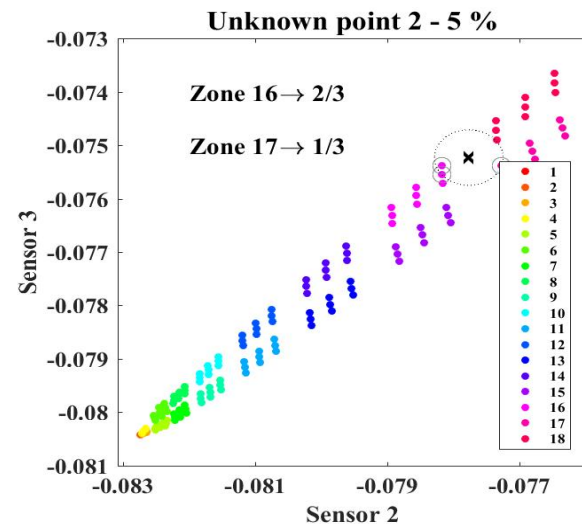
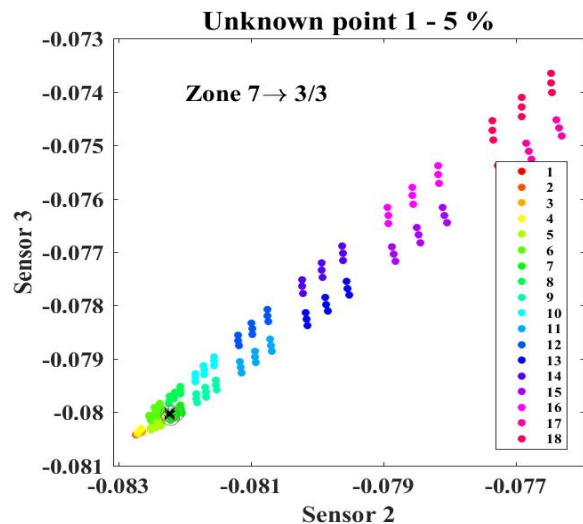
**Point 1 – zone 17**

**Point 1 – zone 7**

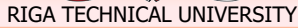
**Point 2 – between zones  
9, 10, 11 and 12**

**Point 2 – between zones  
16 and 18**

*k*-NN search







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### Unknown point 1 – Zone 7

## Unknown point 2 – Zone 18



## Unknown point 1 – Zone 17

## Unknown point 2 – Zone 9



- The damage localization methodology for plate structures based on data classification with  $k$ -NN and decision trees is proposed.
- Classification parameters are optimized to minimize the resubstitution and cross-validation errors.
- The performance of classifiers is assessed through ROC curves with accompanying AUC metric and confusion matrices. These metrics suggest a high quality of classification.
- It is found that there is a good agreement between the localization results of both classifiers and these results are in accordance with the actual coordinates of query points for both severities of damage (5 % and 10 %).

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**Thank You for your attention!**



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